

$$\begin{aligned} \epsilon_{si} &= 1035,45 \text{ fFcm}^{-1} \\ [F] &= [C]/[V] \quad [A] = [C]/[s] \\ n_i &= \sqrt{n_0 \cdot p_0} = [cm^{-3}] \quad (n_0 = p_0 = n_i \text{ intríns.}) \\ &= 2 \left(\frac{2\pi \cdot \sqrt{m_n^* \cdot m_p^*} \cdot kT}{h^2} \right)^{3/2} \exp \left(\frac{-Eg}{2kT} \right) \\ n_0 &= \frac{N_D - N_A}{2} + \sqrt{\left(\frac{N_D - N_A}{2} \right)^2 + n_i^2} \\ &\uparrow \text{para } p_0 \text{ cambiar los D y A} \end{aligned}$$

$$\begin{aligned} v_{th} &= \sqrt{\frac{kT}{m^*}} \quad \text{vel term} \mid v_{p/n}^a = \pm \mu_{p/n} \vec{E} \\ J &= \frac{I}{A} = n \cdot q \cdot v^a \quad R = \frac{L \cdot \rho}{A} = \frac{L}{A \cdot \sigma} \\ J_{n/p}^a &= n/p_0 q \mu_{n/p} \vec{E} \quad J_{n/p}^d = \pm q D_{n/p} \frac{dn/p(x)}{dx} \\ J^a &= J_n^a + J_p^a = \sigma \cdot \vec{E} \quad \sigma = q \cdot (n \mu_n + p \mu_p) \\ D_{p/n} &= \frac{\lambda^2}{2\tau_c} = \mu_{p/n} V_{th} \quad J_n = J_n^a + J_n^d = 0 \\ V_{th} &= (kT)/q \approx 25,9 \text{ mV} \quad \rho(x) = q [N_D - n_0(x)] \\ \phi(x) &= 60 \text{ mV} \cdot \log_{10}(n(x)/n_i) \\ \text{Rel Boltzman} \quad \phi_{n/p} &= \pm V_{th} \cdot \ln \frac{n/p_0}{n_i} \end{aligned}$$

PN

$$\begin{aligned} \text{Zona P/N} \quad \rho &= \mp q N_{A/D} \quad N_A x_{p_0} = N_D x_{n_0} \\ \text{Zona P/N} \quad E(x) &= \mp \frac{q N_{A/D}}{\epsilon_{si}} (x \pm x_{p/n_0}) \\ \phi_B &= \phi_n - \phi_p = V_{th} \cdot \ln (N_A \cdot N_D / n_i^2) \\ \text{SCR-P/N} \quad \phi(x) &= \phi_{p/n} \pm \frac{q N_{A/D}}{2\epsilon_{si}} (x \pm x_{p/x_0})^2 \end{aligned}$$

$$\begin{aligned} \text{Limites región de vaciamiento} \parallel \vec{E} \text{ en juntura} \\ x_{n/p_0} &= \sqrt{(2\epsilon_{si}\phi_B N_{A/D})/(q(N_A + N_D)N_{D/A})} \\ |E_0| &= \sqrt{(2q\phi_B N_A N_D)/(\epsilon_{si}(N_A + N_D))} \\ x_{d_0} &= x_{n_0} + x_{p_0} = \sqrt{2\epsilon_{si}\phi_B(N_A + N_D)/qN_A N_D} \\ [x_n, x_p, x_d, |E|] &= [x_n, x_p, x_d, |E|]_0 \sqrt{1 - (V/\phi_B)} \end{aligned}$$

$$\text{Capacidad de Juntura} \quad C_j(V) = C'_j \cdot A$$

$$C'_j = \sqrt{\frac{q\epsilon_{si}N_A N_D}{2(\phi_B - V)(N_A + N_D)}} = \frac{C'_{j_0}}{\sqrt{1 - (\mathbf{V}/\phi_B)}}$$

$$\text{Diodo PN } V > 0 \Rightarrow |E_{SCR}| \downarrow \Rightarrow |J_a| \downarrow < |J_d|$$

$$n(-x_p) = \frac{n_i^2}{N_A} \exp \left(\frac{V}{V_{th}} \right); p(x_n) = \frac{n_i^2}{N_D} \exp \left(\frac{V}{V_{th}} \right)$$

$$J_{n/p} = q \frac{n_i^2}{N_{A/D}} \frac{D_{n/p}}{W_{p/n} - x_{p/n}} \left(\exp \left(\frac{V}{V_{th}} \right) - 1 \right)$$

$$\text{Directa: } V_D = V_{D(on)} \quad I_D > 0 \quad C_{dif} \gg C_j; r_d \downarrow$$

$$\begin{aligned} \text{Inver: } V_D &\neq V_{D(on)}; I_D \simeq -I_0; r_d \rightarrow \infty; C_{dif} \rightarrow 0 \\ I_D &= I_0 \left(\exp \left(\frac{V}{n \cdot V_{th}} \right) - 1 \right) \quad I_{0(gen)} = \frac{qAn_i x_d(V)}{\tau_g} \\ I_0 &= qAn_i^2 \left(\frac{D_n}{N_A(W_p - x_p)} + \frac{D_p}{N_D(W_n - x_n)} \right) \\ v_D(t) &= V_D + v_d(t) \quad i_D(t) = I_D + g_d \cdot v_d(t) \\ g_d &= (I_D + I_0)/V_{th} \quad C_{dif} = \tau_T \cdot g_d \\ \tau_{T_{p/n}} &= \frac{(W_{n/p} - x_{n/p})^2}{2D_{p/n}} \quad \tau_T = \frac{\tau_{T_p} I_{D_p} + \tau_{T_n} I_{D_n}}{I_D} \end{aligned}$$

Juntura MOS

$$\begin{aligned} \text{sustP: } V_T &> 0 \quad \text{gateN}^{++}: V_{FB} < 0 \\ \phi_B + V_{GB} &= \Delta V_{ox} + \Delta V_{bulk} \quad (N/P)^{++} \phi_G = \pm 550 \text{ mV} \\ C'_{ox} &= \epsilon_{ox}/t_{ox} \quad C_{vac} = \epsilon_{si}/x_d \\ \text{Vaciamiento: } Q'_G &= -Q'_{bulk} = qN_{bulk} x_d(V_{GB}) \\ x_d(V) &= \epsilon_{sc} \left(\sqrt{1 + 4(\phi_B - V)\gamma^{-2}} - 1 \right) / C'_{ox} \\ \gamma &= \sqrt{2\epsilon_{si}qN_{bulk}} / C'_{ox} \quad \Delta V_{bulk} = qN_{bulk} x_d^2(V_{GB}) / 2\epsilon_{sc} \\ \Delta V_{ox} &= Q_G / C'_{ox} = qN_{bulk} t_{ox} x_d(V_{GB}) / \epsilon_{ox} \\ \text{Flatband: } V_{GB} &= -\phi_B = V_{FB} \\ \vec{E} &= \phi(x) = \Delta V_{bulk} = \Delta V_{ox} = x_d = 0 \\ \text{Acumulacion} \quad Q'_{ac} &= -Q'_{gate} = -C'_{ox} \Delta V_{ox} \\ x_d &= \Delta V_{bulk} = 0 \quad \Delta V_{ox} = V_{GB} - V_{FB} \\ \text{Tensión Umbral}(V_T) \quad \Delta V_{bulk} &= -2\phi_p \\ \Delta V_{ox} &= \gamma \sqrt{-2\phi_p} = 2\phi_B + V_{GB} - \Delta V_{bulk} \\ \text{Inversión} \quad Q'_{gate} &= -Q'_{bulk} - Q'_{inv} = \\ &= qN_A x_d(V_T) + C'_{ox}(V_{GB} - V_T) \\ \text{Capacidad de MOS} \quad C'_{GB} &= C'_{ox} \text{ acu/inv} \end{aligned}$$

$$C'_{GB} = \frac{C'_{vac} C'_{ox}}{C'_{vac} + C'_{ox}} = \frac{C'_{ox}}{\sqrt{1 + \frac{4(\phi_B + V_{GB})}{\gamma^2}}} \text{ vac.}$$

Transistor MOSFET (N/P)

$$V_{DS_{sat}} = V_{GS} - V_T \quad k = (\mu_n C'_{ox} W)/(2L)$$

$$\text{Corte: } V_{GS} \leqslant V_T \quad I_D = 0$$

$$\text{Saturación: } V_{GS} \geqslant V_T \quad V_{DS} \geqslant V_{DS_{sat}}$$

$$I_D = \pm k(V_{GS} - V_T)^2 [1 \pm \lambda V_{DS}]$$

$$\text{Triodo: } V_{GS} \geqslant V_T \quad V_{DS} \leqslant V_{DS_{sat}}$$

$$I_D = \pm 2k(V_{GS} - V_T - (V_{DS}/2)) V_{DS} [1 \pm \lambda V_{DS}]$$

$$\text{-Back: } V_T = V_{FB} - 2\phi_{p/n} \pm \gamma \sqrt{\mp(2\phi_{p/n} + V_{BS})}$$

$$\text{MPS: } i_D = k(V_{GS} - V_T)^2 + 2k(V_{GS} - V_T) \cdot v_{gs}(t)$$

$$g_m = 2k(V_{GS} - V_T) \quad r_0 = 1/2k(V_{GS} - V_T)^2 \lambda$$

$$g_{mb} = g_m(\gamma/2\sqrt{-2\phi_B - V_{BS}}) \quad C_{gd} = WC_{ov}$$

$$C_{gs} = (2/3)WL C'_{ox} + C_{gd} \quad C_{sb/db} = A_{s/d} C'_j$$